

Quantum systems of ultracold atoms  
New probes of many-body correlations

## Analysis of quantum noise

Interference of fluctuating condensates and  
correlation functions

From quantum noise to high  
order correlation functions

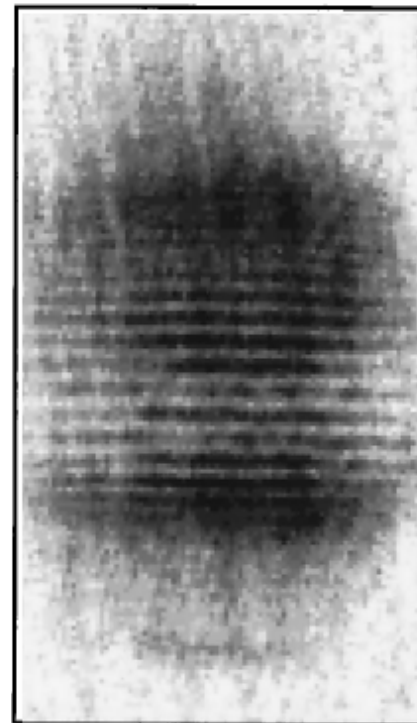
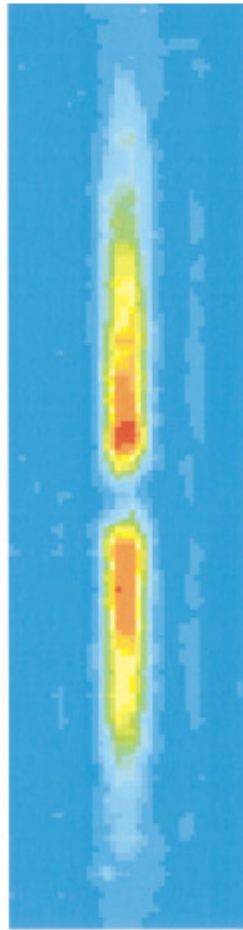
Analysis of magnetization  
fluctuations in lattice models



**MURI**  
Program in  
Optical Lattices

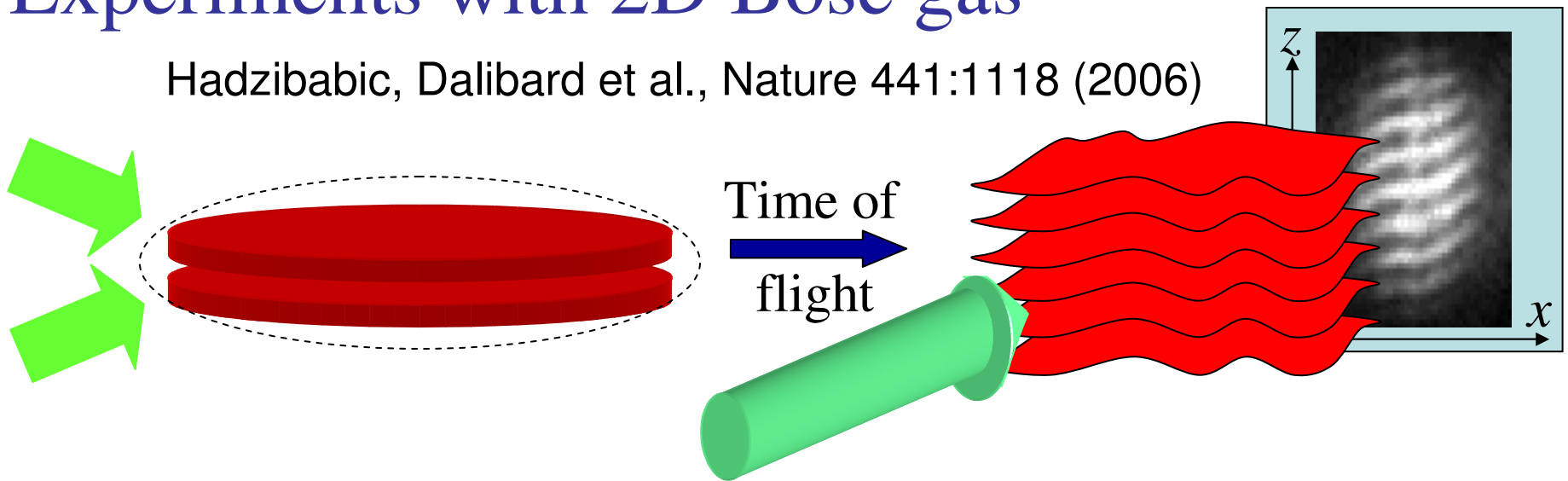
# Interference of two independent condensates

Andrews et al., Science 275:637 (1997)

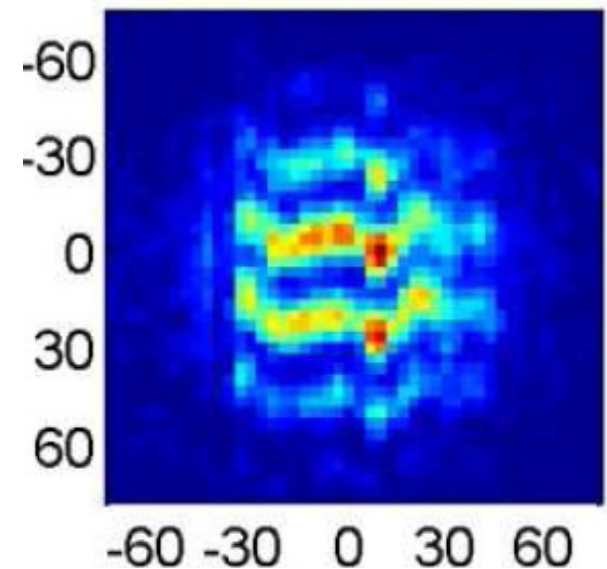
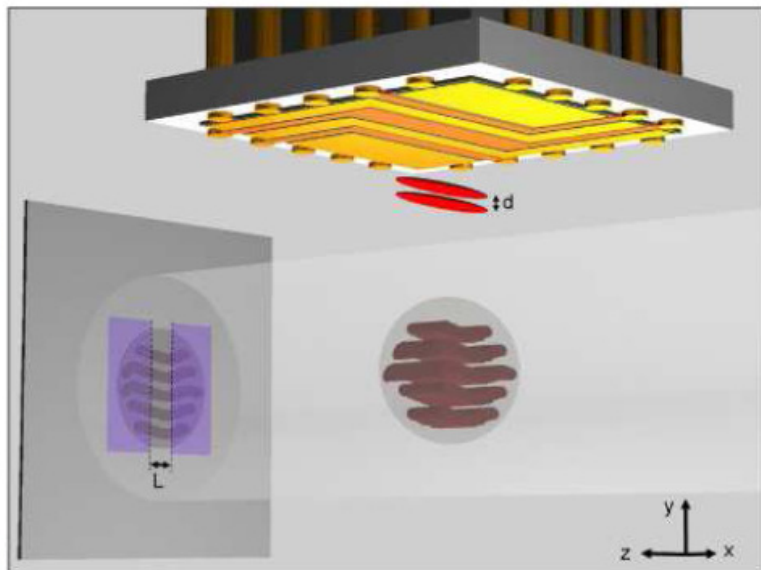


# Experiments with 2D Bose gas

Hadzibabic, Dalibard et al., Nature 441:1118 (2006)

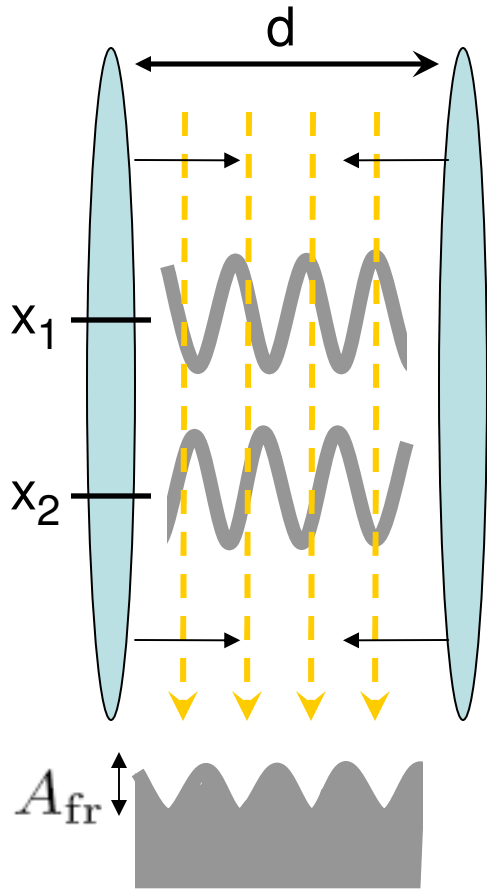


# Experiments with 1D Bose gas S. Hofferberth et al. arXiv0710.1575



# Interference of fluctuating condensates

Polkovnikov, Altman, Demler, PNAS 103:6125(2006)



Amplitude of interference fringes,  $A_{fr}$

$$|A_{fr}| e^{i\Delta\phi} = \int_0^L dx a_1^\dagger(x) a_2(x)$$

For independent condensates  $A_{fr}$  is finite but  $\Delta\phi$  is random

$$\begin{aligned} \langle |A_{fr}|^2 \rangle &= \int_0^L \int_0^L dx dy \langle a_1^\dagger(x) a_2(x) a_2^\dagger(y) a_1(y) \rangle \\ &\simeq L \int_0^L dx \langle a_1(x) a_1^\dagger(0) \rangle \langle a_2(0) a_2^\dagger(x) \rangle \end{aligned}$$

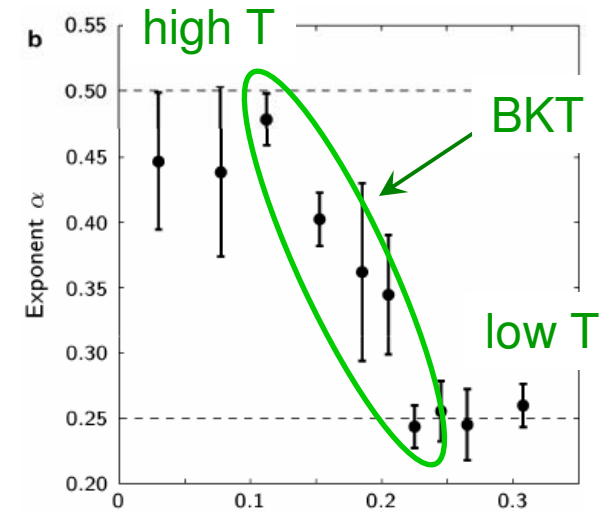
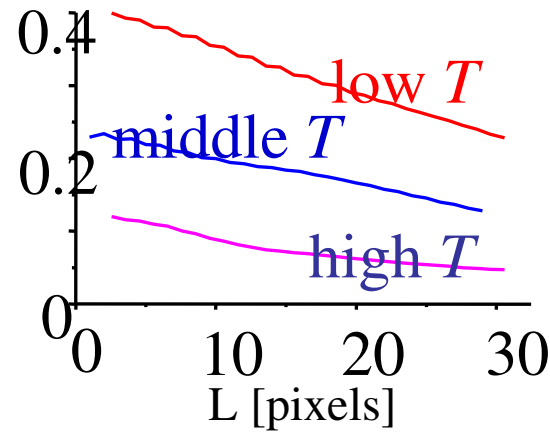
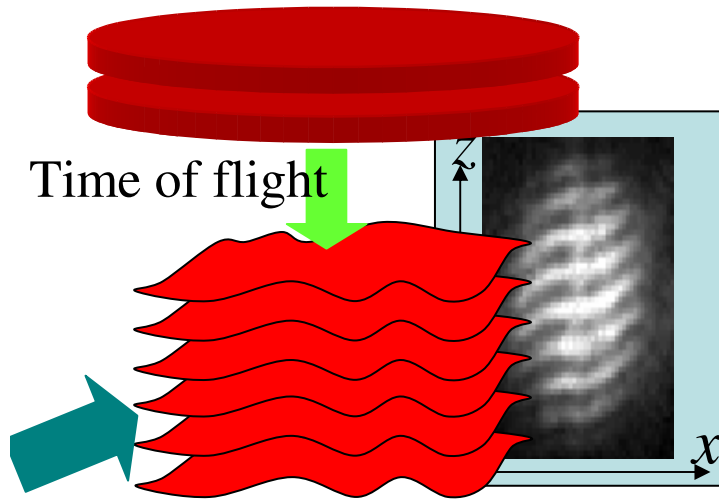
For identical condensates

$$\langle |A_{fr}|^2 \rangle = L \int_0^L dx (G(x))^2$$

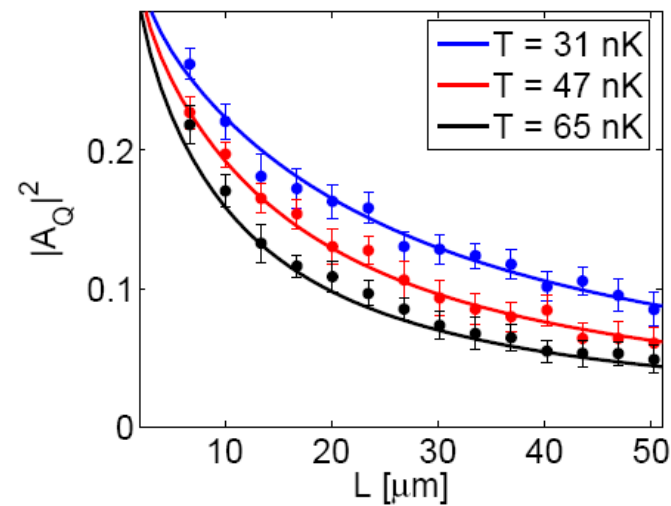
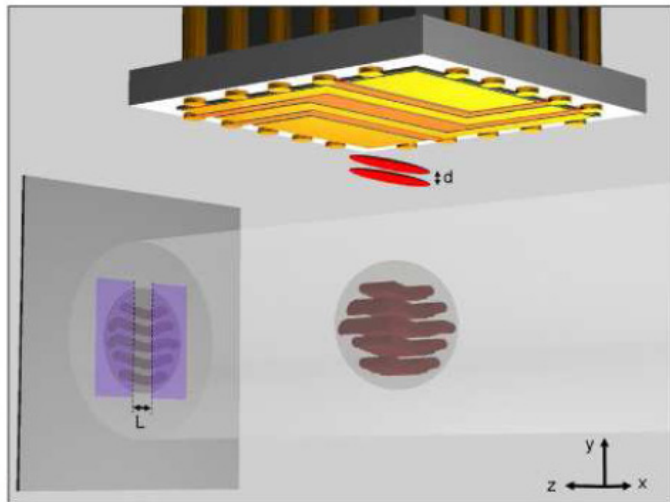
Instantaneous correlation function

$$G(x) = \langle a(x) a^\dagger(0) \rangle$$

# Interference between fluctuating condensates



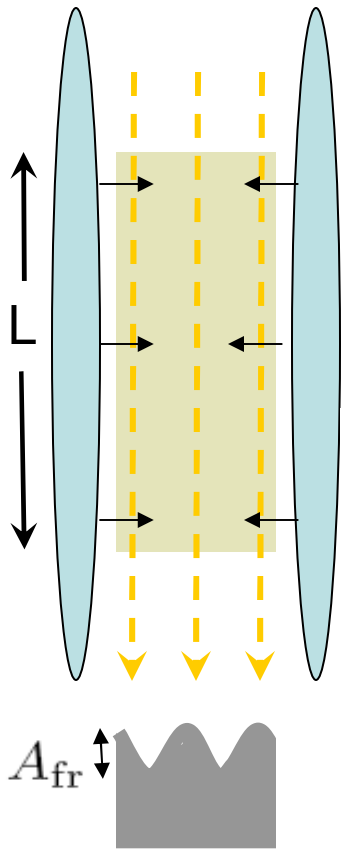
2d: BKT transition, Hadzibabic et al, 2006



1d: Luttinger liquid, Hofferberth et al., 2007

# Distribution function of fringe amplitudes for interference of fluctuating condensates

Gritsev, Altman, Demler, Polkovnikov, Nature Physics 2006  
Imambekov, Gritsev, Demler, cond-mat/0612011



$A_{\text{fr}}$  is a quantum operator. The measured value of  $|A_{\text{fr}}|$  will fluctuate from shot to shot.

$$\langle |A_{\text{fr}}|^{2n} \rangle = \int_0^L dz_1 \dots dz'_n |\langle a^\dagger(z_1) \dots a^\dagger(z_n) a(z'_1) \dots a(z'_n) \rangle|^2$$

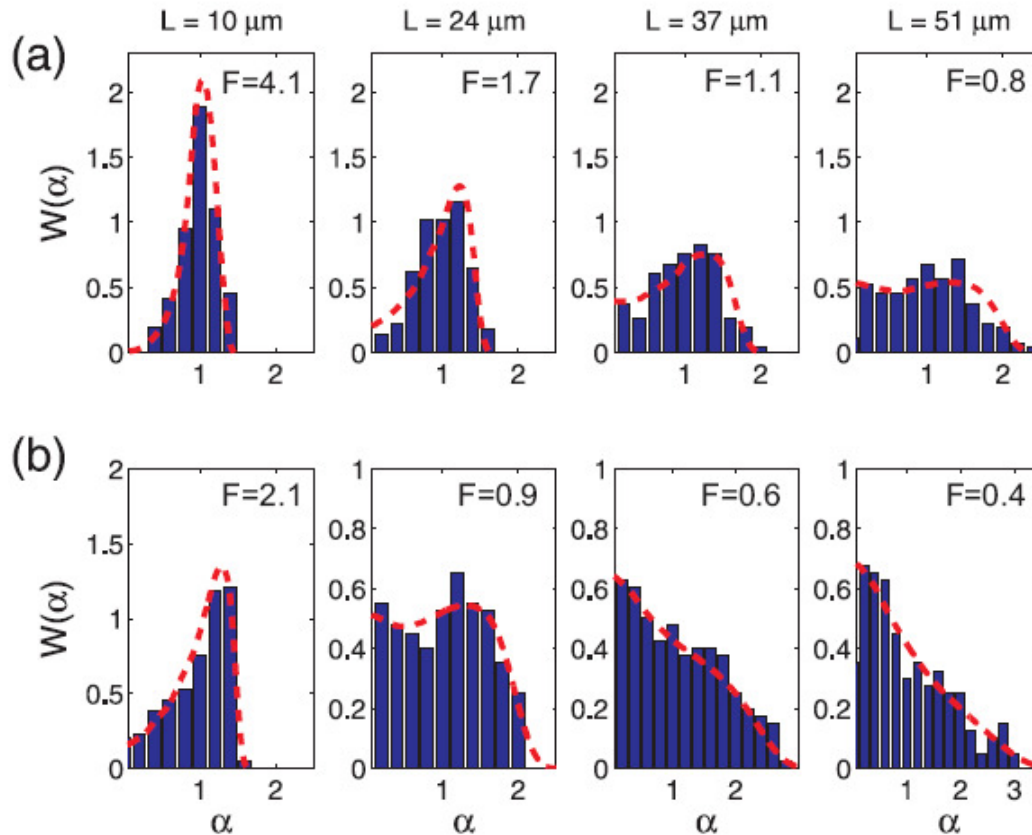
Higher moments reflect higher order correlation functions

We need the full distribution function of  $|A_{\text{fr}}|$

# Distribution function of interference fringe contrast

Experiments: Hofferberth et al., arXiv0710.1575

Theory: Imambekov et al. , cond-mat/0612011



**Quantum fluctuations** dominate:  
asymmetric Gumbel distribution  
(low temp.  $T$  or short length  $L$ )

**Thermal fluctuations** dominate:  
broad Poissonian distribution  
(high temp.  $T$  or long length  $L$ )

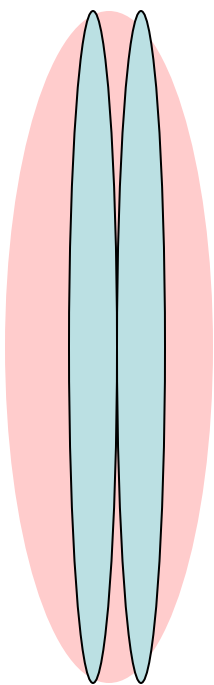
**Intermediate regime:**  
double peak structure

Comparison of theory and experiments: no free parameters  
Higher order correlation functions can be obtained

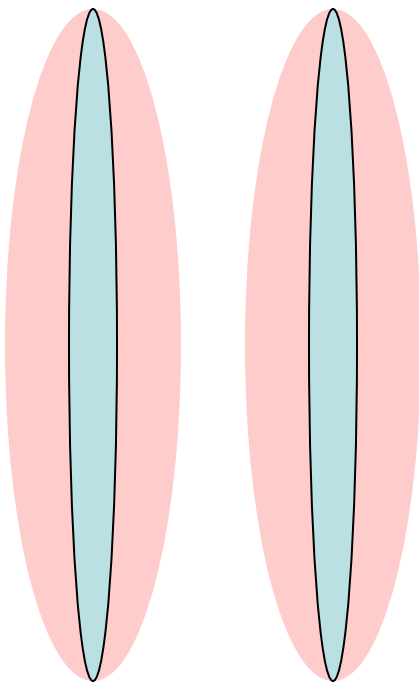
Studying coherent dynamics  
of strongly interacting systems  
in interference experiments



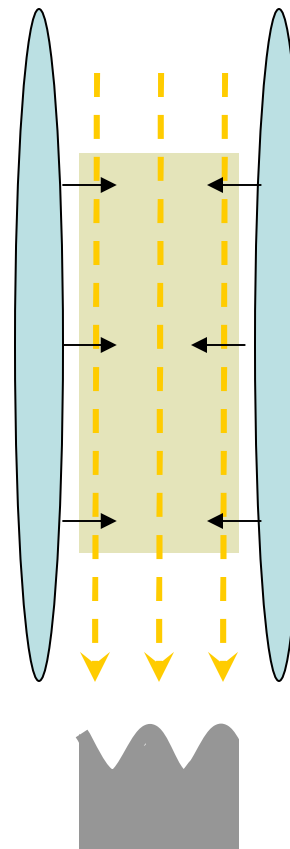
# Studying dynamics using interference experiments



Prepare a system by splitting one condensate



Take to the regime of zero tunneling

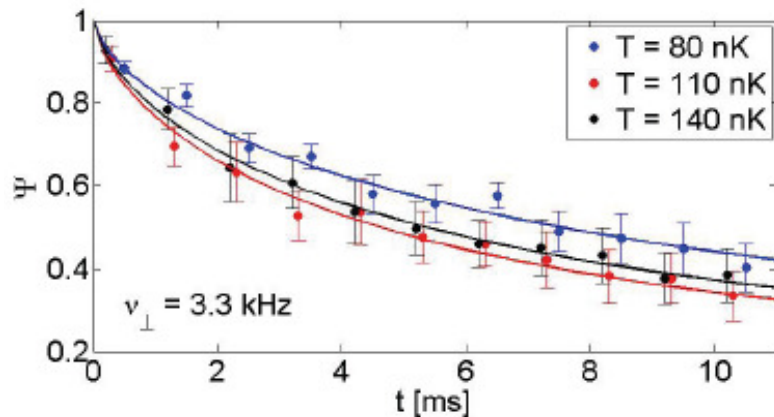
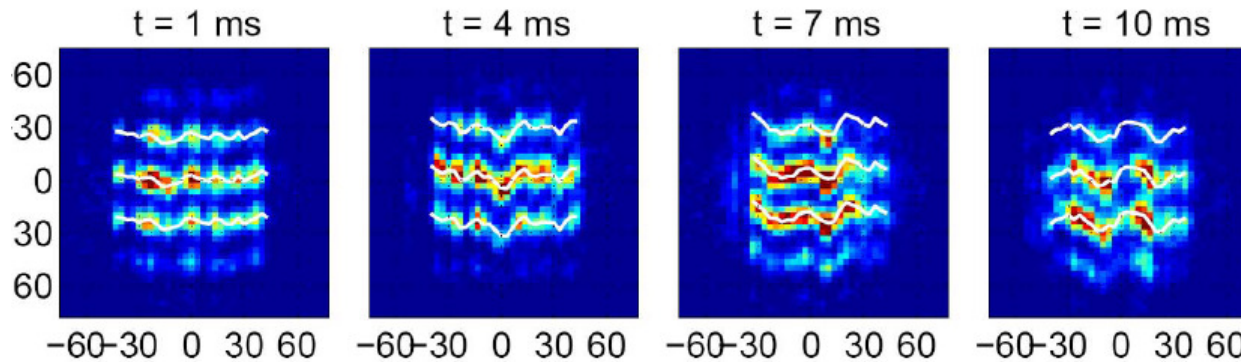


Measure time evolution of fringe amplitudes

# Dynamics of split condensates

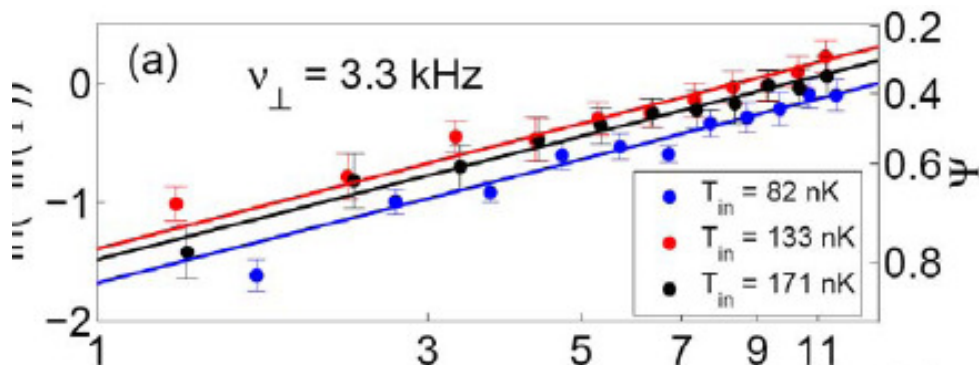
Theory: Burkov et al., PRL 2007

Experiment: Hofferberth et al., Nature 2007



Theoretical prediction

$$\langle e^{i\phi(t)} \rangle \sim e^{-\left(\frac{t}{t_T}\right)^{2/3}}$$

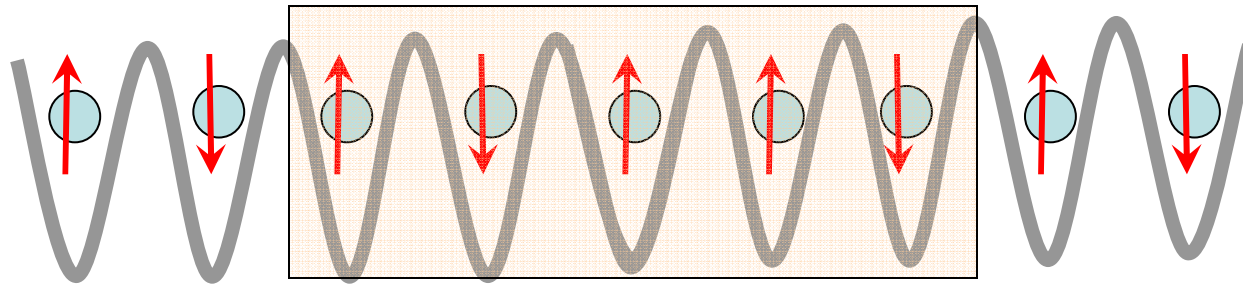


$T_{in}$ [nK]	$n_{1d}$ [1/ $\mu\text{m}$ ]	$\omega_{\perp}$ $2\pi$ [kHz]	$\alpha$
82(28)	20(4)	3.3	0.64(8)
133(25)	34(5)	3.3	0.65(7)
171(19)	52(4)	3.3	0.64(4)
81(31)	22(4)	4.0	0.65(3)
128(23)	37(4)	4.0	0.66(3)
175(20)	51(5)	4.0	0.64(6)

Probing spin systems using  
distribution function of magnetization

# Probing spin systems using distribution function of magnetization

Cherng, Demler, New J. Phys. 9:7 (2007)



Magnetization in a finite system

$$M_{\text{tot}}^z = \sum_{i=1}^L M^z(i)$$

Average magnetization

$$\langle M_{\text{tot}}^z \rangle = L \langle M^z \rangle$$

Higher moments of  $M_{\text{tot}}^z$  contain information about higher order correlation functions

$$\langle (M_{\text{tot}}^z - \langle M_{\text{tot}}^z \rangle)^2 \rangle = L \sum_{ij} \langle (M_z(i) - \langle M^z \rangle) (M^z(j) - \langle M^z \rangle) \rangle$$

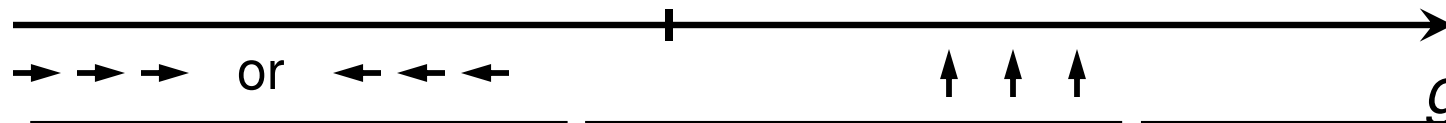
# Distribution Functions

$$\mathcal{H} = -J \sum_i [2S^x(i)S^x(i+1) + gS^z(i)]$$

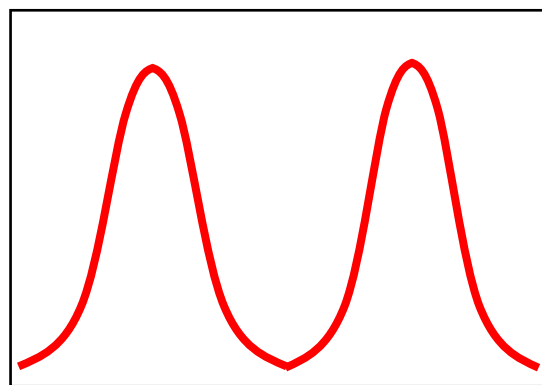
x-Ferromagnet

1

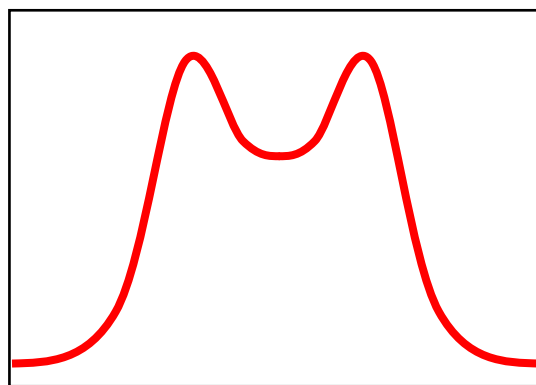
polarized



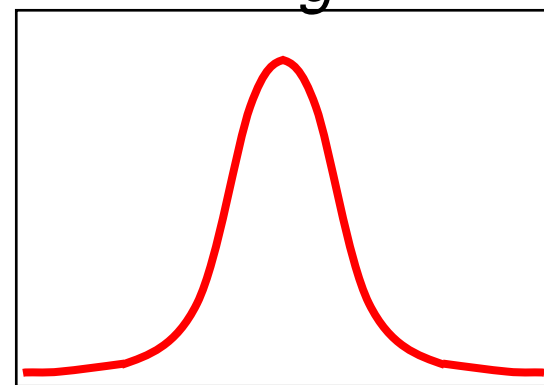
$P(m_x)$



$m_x$

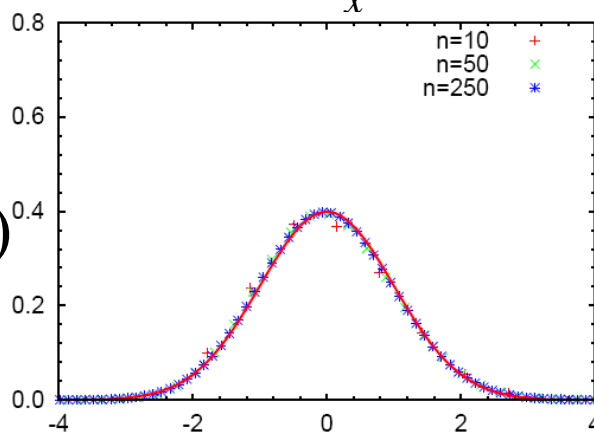


$m_x$

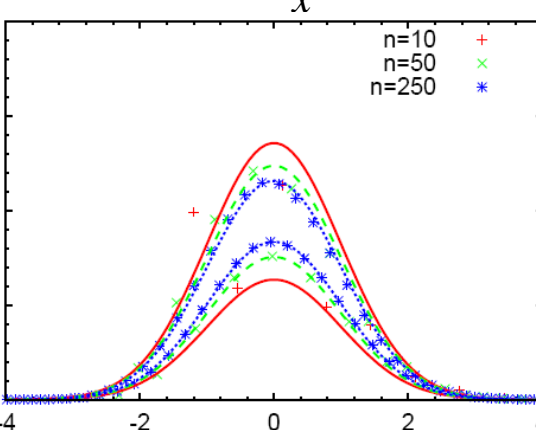


$m_x$

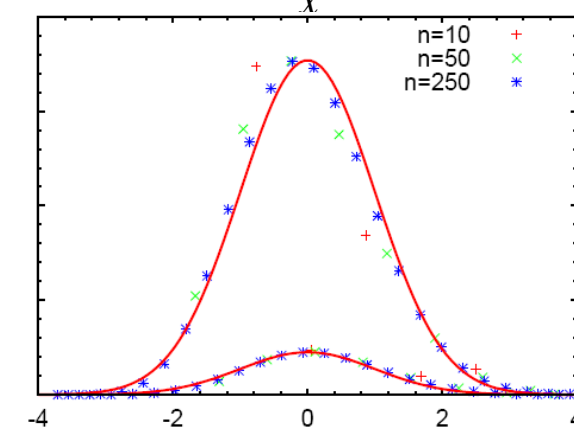
$P(m_z)$



$m_z - \langle m_z \rangle$

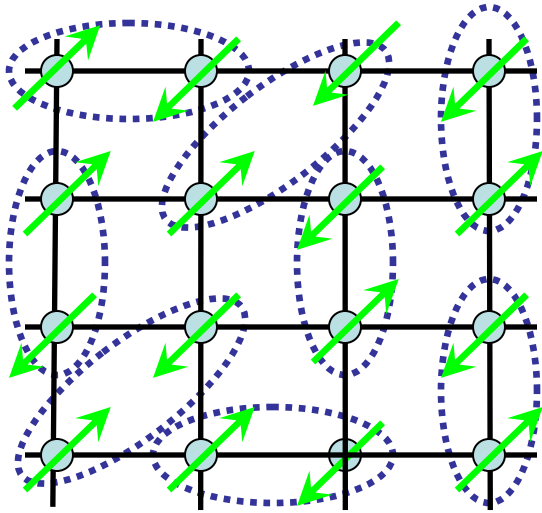


$m_z - \langle m_z \rangle$



$m_z - \langle m_z \rangle$

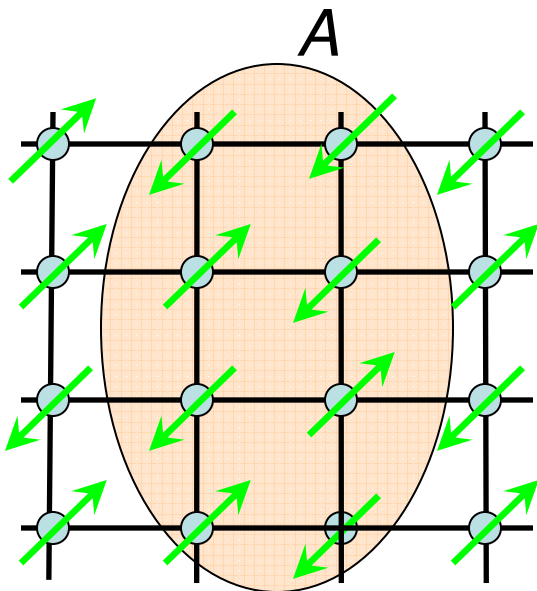
# Using noise to detect spin liquids



Spin liquids have no broken symmetries  
No sharp Bragg peaks

Algebraic spin liquids have long range  
spin correlations

$$\langle S_i S_j \rangle = \frac{e^{iQ r_{ij}}}{|r_i - r_j|^{1+\eta}}$$



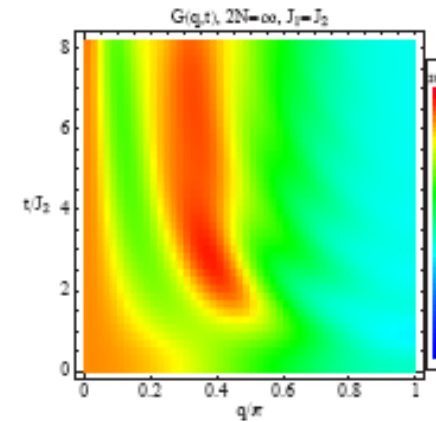
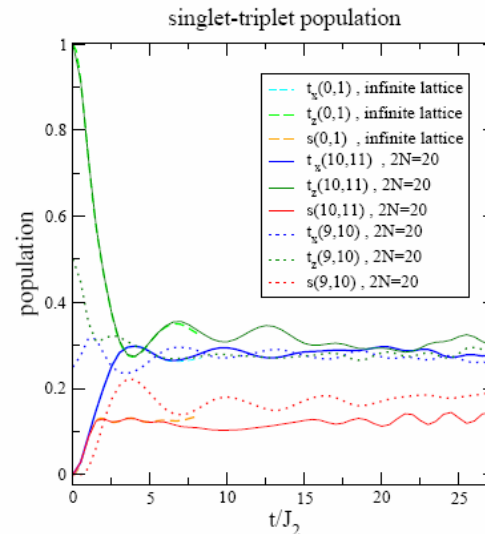
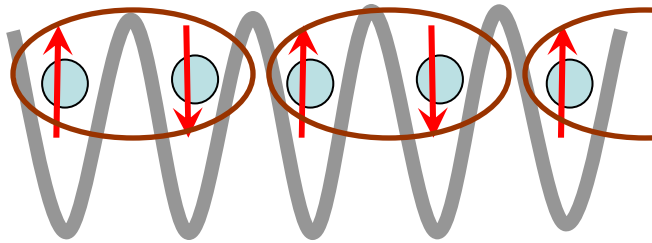
No static magnetization  $\langle S_A \rangle = 0$

Noise in magnetization exceeds shot noise

$$\langle S_A^2 \rangle = \sum_{ij} \langle S_i S_j \rangle \sim A \int_A \frac{r dr}{|r|^{1+\eta}} \sim A^{1+\frac{1-\eta}{2}}$$

# Work in progress on theoretical milestones for MURI

Investigate coherent quantum dynamics of strongly interacting spin systems and superfluids



Investigate experimental requirements for reaching and detecting the antiferromagnetic phase  
(Long lived doublon states)

Investigate theoretically new approaches to realizing and detecting of spin liquid states and anyon statistics  
(Measuring spin loop operators using coupling to cavity)

# MURI quantum simulation project

## Phase I

### **Validation and Verification**

Simulate solvable Hamiltonians. Compare with calculations.

Examples: low dimensional systems, precision study of Mott insulator phases, superexchange interactions, fermionic superfluidity in optical lattice.

### **New tools for detection and characterization of strongly correlated states**

Optical addressability → Quantum gas microscope

Critical velocity in moving superfluids

Bragg spectroscopy in optical lattices

Quantum noise analysis

## Phase II

*Combine all tools and methods developed during phase I to tackle goals of this MURI project:*

**Quantum magnetism**

**Fermionic superfluidity in systems with repulsive interactions**

**Ultimate goal: use the results of quantum analogue simulations to identify new solid state systems with favorable properties**

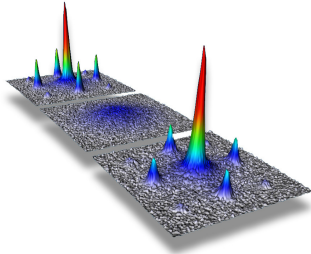


# *Quantum Simulations of Condensed Matter Systems using Ultracold Atomic Gases*

*FY07 MURI Topic #18*

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Luming Duan, Mark Kasevich, Wolfgang Ketterle, Mikhail Lukin,  
Subir Sachdev, Martin Zwierlein, Joseph Thywissen, Immanuel Bloch,  
Peter Zoller

Collaborating Universities: Harvard, MIT, Stanford, Michigan,  
Toronto, University of Mainz, Germany, University of Innsbruck,



**MURI**  
Program in  
Optical Lattices

